

## The Saylor Foundation's

### ME103 Assessment, Unit 2: Guide to Responding

**Instructions:** Please answer each of the following questions to the best of your ability.

#### Questions:

1. Estimate the pressure of one kmol of ethylene contained in a  $0.6 \text{ m}^3$  volume and at temperature  $200^\circ\text{C}$  using (a) ideal gas law and (b) van der Waal's equation, with  $a = 453.046 \times 10^{-3} \text{ Pa}(\text{m}^3/\text{mol})^2$  and  $b = 0.057 \times 10^{-3} \text{ m}^3/\text{mol}$ .
2. Determine the compressibility factor and molar volume for a gas at 500 K and 10 bar, which obeys the truncated virial equation:  $PV/RT = 1 + B/V + C/V^2$ , with  $B = -2.2 \times 10^{-4} \text{ m}^3/\text{mol}$ ;  $C = -1.7 \times 10^{-8} \text{ m}^6/\text{mol}^2$ . The critical temperature and pressure of the gas are 515 K and 81 bar.
3. Calculate the volume of one kilo mol of gas at 51.8 bar and 313 K using the van der Waal's equation. The van der Waals constants for the gas are  $a = 0.365 \text{ Nm}^4/\text{mol}^2$  and  $b = 4.28 \times 10^{-5} \text{ m}^3/\text{mol}$ .

#### Solutions:

1. a) According to ideal gas law,  $PV = RT$ . Hence,  $P = RT/V = 8.314 \times 10^3 \times 473 / 0.6 = 6.5 \text{ MPa}$   
b) Van der Waal's equation:  $P = RT/v - b - a/v^2$ . This gives  $P = 6.0 \text{ MPa}$
2. The compressibility factor is defined as  $Z = PV/RT = 1 + B/V + C/V^2$ . Thus, knowing  $V$  will allow us to calculate  $Z$ . To calculate  $Z$ , we will need to use an iterative procedure to solve

$$V = RT/P(1 + B/V + C/V^2)$$

We can use the ideal gas volume ( $V = RT/P$ ) as the initial guess. After obtaining  $V$ , we solve for  $Z$  and obtain  $Z = 0.94$ .



3. The Van der Waals equation is  $P = \frac{RT}{V - b} - \frac{a}{V^2}$ . We know T and P. To obtain V, use an iterative procedure to solve for V using the ideal gas volume as the initial guess. This will give  $V = 0.38 \text{ m}^3$ .

