

  integer factorization(Definition)

Given an [integer](#)  $n$ , its *integer factorization* (or *prime factorization*) consists of the [primes](#)  $p_i$  which multiplied together give  $n$  as a result. To put it algebraically,

$$n = \prod_{i=1}^{\omega(n)} p_i^{a_i},$$

with each  $p_i$  distinct, all  $a_i > 0$  but not necessarily distinct, and  $\omega(n)$  being the value of the [number of distinct prime factors function](#). Theoretically, an integer is a [product](#) of all the prime numbers,

$$n = \prod_{i=1}^{\infty} p_i^{a_i},$$

with many  $a_i = 0$ .

For example, the factorization of 32851 is  $7 \times 13 \times 19 \times 19$ , more usually expressed as  $7 \times 13 \times 19^2$ . Because of the [commutative property](#) of [multiplication](#), it does not matter in what [order](#) the [prime factors](#) are stated in, but it is customary to give them in [ascending order](#), and to [group](#) them together by the use of [exponents](#).

The factorization of a [positive](#) integer is unique (this is the [fundamental theorem of arithmetic](#)). For a [negative number](#)  $n < 0$  one could take the factorization of  $|n|$  and randomly give [negative](#) signs to one (or any [odd number](#)) of the prime factors. Alternatively, the factorization can be given as  $-1 \cdot p_1^{a_1} \dots$  (this is what [Mathematica](#) opts for).

The [term](#) "factorization" is often used to refer to the actual process of determining the prime factors. There are several [algorithms](#) to choose from, with [trial division](#) being the simplest to implement.

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**Attachments:**

[trial division](#) (Algorithm) by CompositeFan  
[Fermat method](#) (Algorithm) by PrimeFan

$$p - 1$$

[Pollard's algorithm](#) (Algorithm)  
by PrimeFan

$$\rho$$

[Pollard's algorithm](#) (Algorithm) by  
PrimeFan

[table of integer factorizations](#)

$$0 < n < 1001$$

[for](#) (Data  
Structure) by PrimeFan

[prime signature](#) (Definition) by PrimeFan

Cross-references: [trial division](#), [algorithms](#), [term](#), [Mathematica](#), [odd number](#), [negative](#), [negative number](#), [fundamental theorem of arithmetic](#), [positive](#), [exponents](#), [group](#), [prime factors](#), [order](#), [multiplication](#), [property](#), [commutative](#), [product](#), [number of distinct prime factors function](#), [primes](#), [integer](#)

There are [37 references](#) to this entry.

This is [version 5](#) of [integer factorization](#), born on 2007-02-02, modified 2009-03-21.

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Pending Errata and Addenda

None.

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Discussion

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[Contrasting and comparing PrimeFan, CompositeFan](#) by [Mravinci](#) on 2007-02-22 16:19:39

I just noticed that CompositeFan attached her entry on trial division to the entry on composite numbers, while PrimeFan attached his entry on the Fermat method to the entry on primes. (I think attaching to integer factorization would make more sense).

There are other interesting similarities and differences between the two: PrimeFan will contribute something to Wikipedia first and then PlanetMath, while CompositeFan will contribute something to PlanetMath first and then Wikipedia. PrimeFan is an old man who served in the Navy in the pointful Second World War, while CompositeFan is a young woman who served in the Navy in the pointless First Gulf War. PrimeFan hates classical music but is interested in opus sequences, while CompositeFan loves classical music but couldn't care less for opus sequences. etc.

